

ROHINI COLLEGE OF ENGINEERING AND TECHNOLOGY
Anjugrammam main Road, Palkulam 629401, Kanyakumari District

Department of Electrical and Electronics Engineering

Academic Year (2023-24) (EVEN)

EE3401 – TRANSMISSION AND DISTRIBUTION

ASSIGNMENT RUBRICS

KNOWLEDGE DOMAIN RUBRICS (EE3401)	Marks
Assignment questions have been answered/solved appropriately and submitted on-time.	4
Presentation and sequence representation of the assigned work.	3
Personal view over the assigned work reflecting self-learning aspect.	3
TOTAL	10

ROHINI COLLEGE OF ENGINEERING & TECHNOLOGY,
PALKULAM

Accredited by NAAC with A+ Grade

Department of Electrical and Electronics Engineering

TRANSMISSION AND DISTRIBUTION
<EE3401>

Assignment - 2

S. No.	Assignment Questions	K Level	CO	Mapping of PO/PSO
1	Explain the short transmission line with a neat circuit and phasor diagram.	K2	21C211.2	PO1, PO12, PSO1
2	Outline the medium 'T' transmission line with a neat circuit and phasor diagram.	K2	21C211.2	PO1, PO12, PSO1
3	Outline the medium Π transmission line with a neat circuit and phasor diagram.	K2	21C211.2	PO1, PO12, PSO1
4	Infer the rigorous method of long transmission line with a neat circuit.	K2	21C211.2	PO1, PO12, PSO1
5	Infer the receiving end and sending end power circle diagram with neat sketches and procedures.	K2	21C211.2	PO1, PO12, PSO1

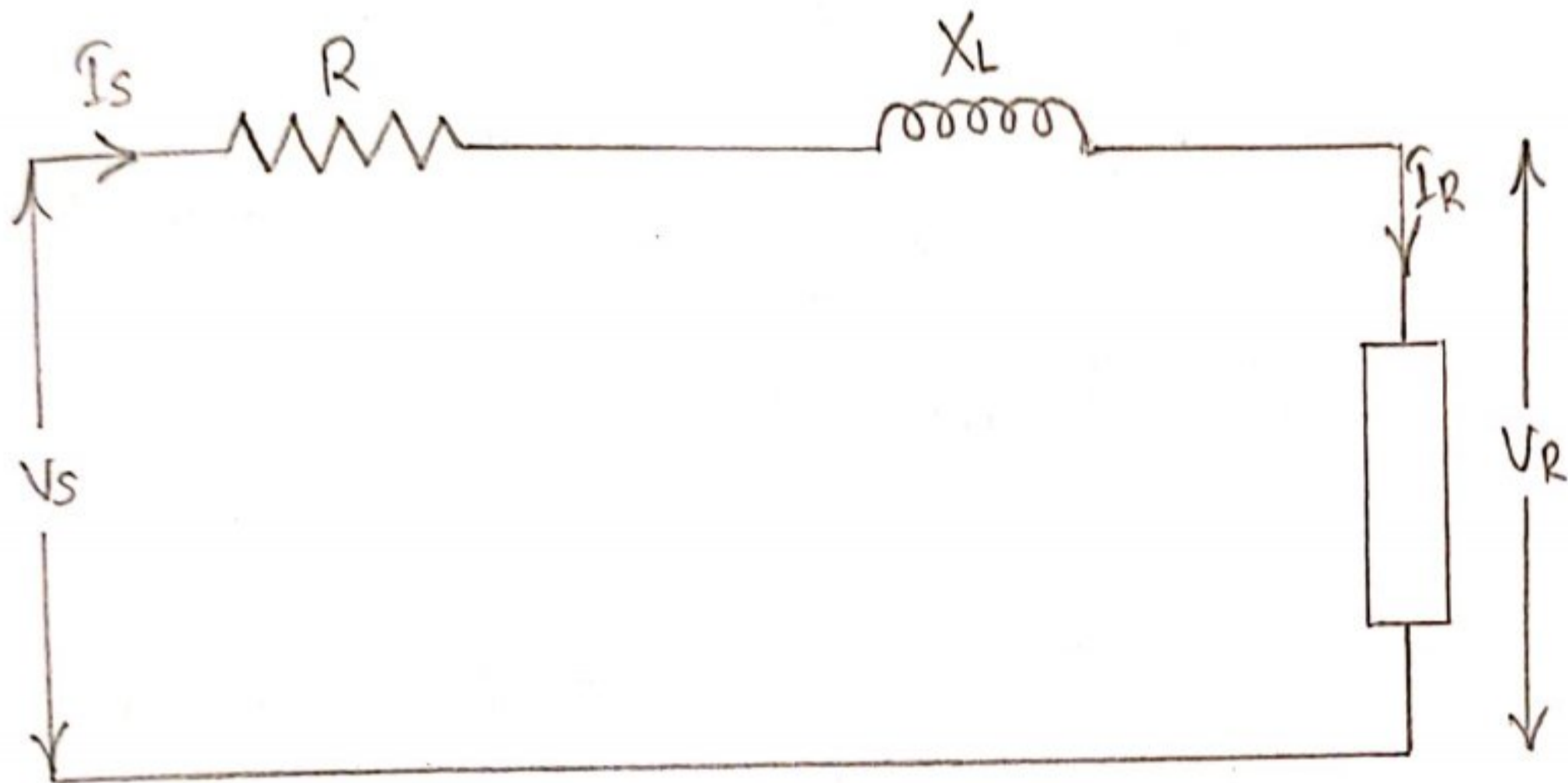
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IIIrd yr EEE
Roll No: 12 / Reg. No. 13

Assignment Date: 29.02.2024
Submission Date: 08-04-24

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A+B+B
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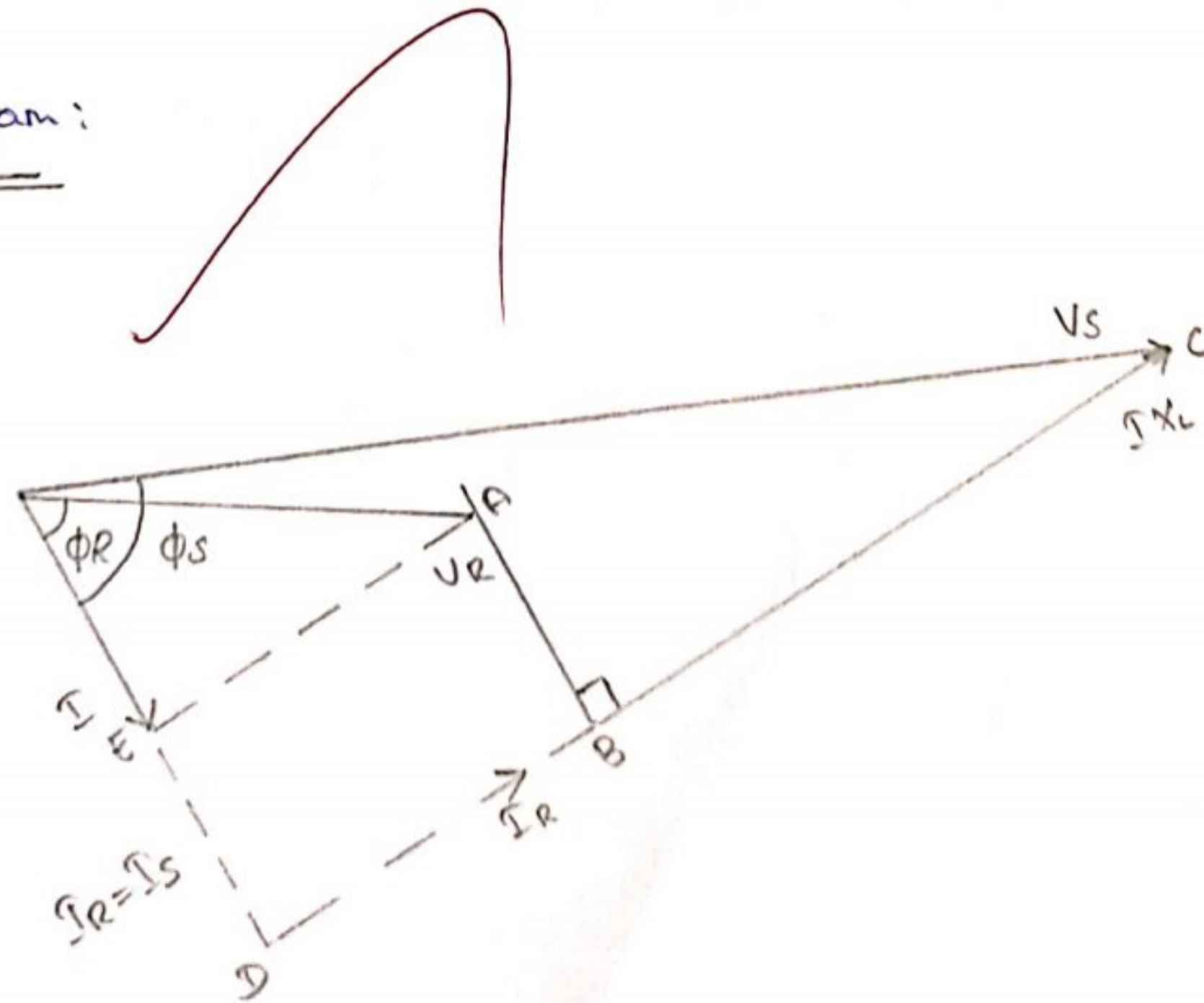
Explain the short transmission line with a neat circuit and phasor diagram.

- (*) Voltage is less than 20kV
- (*) Line length is upto 50 km
- (*) Capacitance neglected.



- Let,
- $I_R \Rightarrow I$ load current
 - $R \Rightarrow$ loop resistance
 - $X_L \Rightarrow$ loop reactance
 - $V_S \Rightarrow$ sending end voltage
 - $V_R \Rightarrow$ receiving end voltage

Phasor Diagram:



From the right angle triangle

ΔODC

$$OC^2 = OD^2 + DC^2$$

$$= (OE + DE)^2 + (OB + BC)^2$$

$$U_s^2 = (U_R \cos \phi_R + I R)^2 + (U_R \sin \phi_R + I X_L)^2$$

$$U_s = \sqrt{(U_R \cos \phi_R + I R)^2 + (U_R \sin \phi_R + I X_L)^2}$$

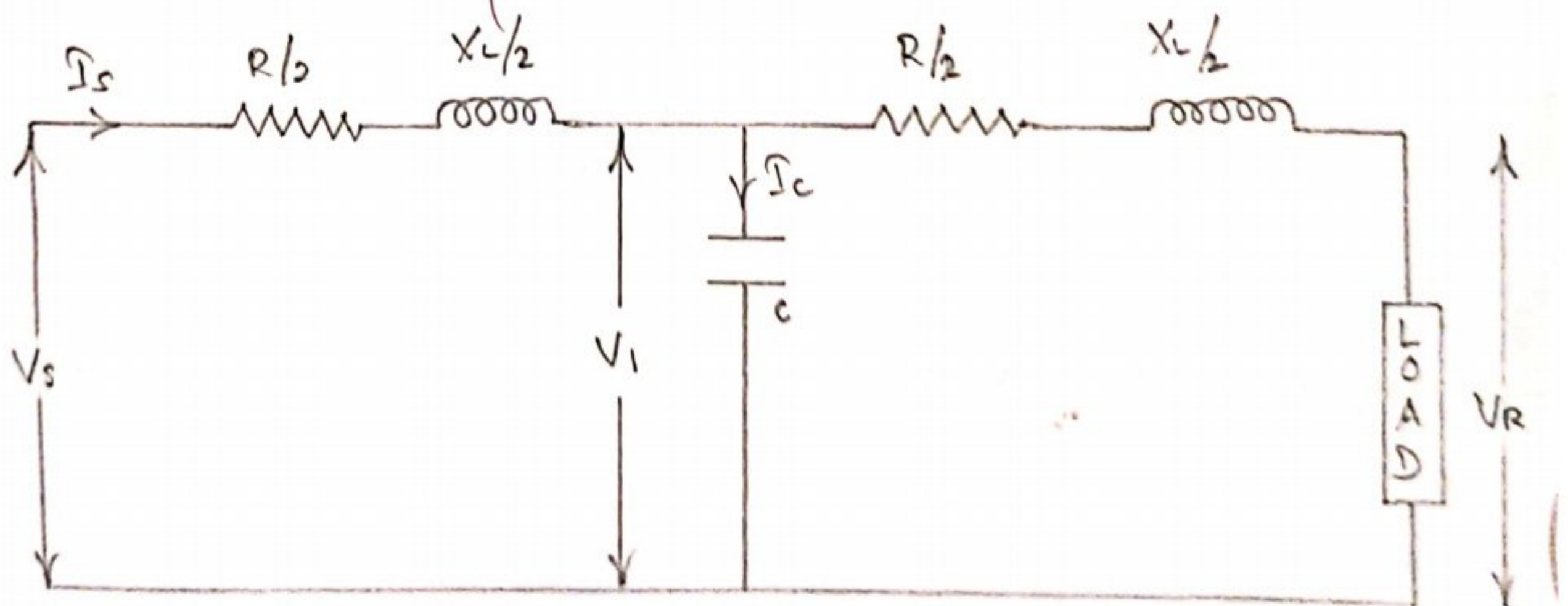
$$\text{① \% Voltage Regulation} = \frac{U_s - U_R}{U_R} \times 100\%$$

$$= \frac{I R \cos \phi_R + I X_L \sin \phi_R}{E_R} \times 100$$

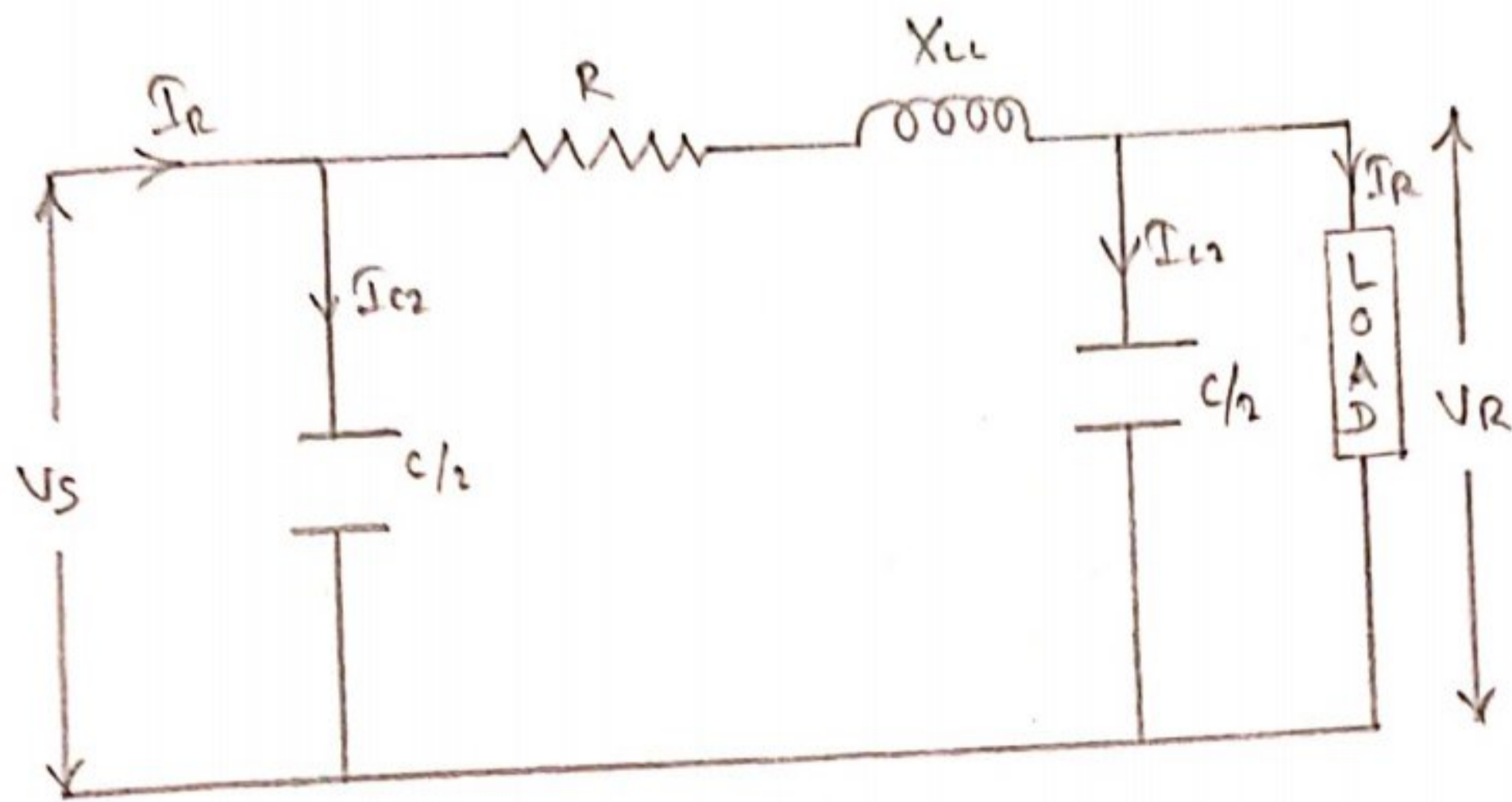
$$\text{② Transmission Efficiency} = \frac{U_R I_R \cos \phi_R}{U_s I_s \cos \phi_s}$$

$$\text{\% Tr. eff} = \frac{U_R I_R \cos \phi_R}{U_R I_R \cos \phi_R + I^2 R} \times 100$$

2. Explain the medium transmission line with neat diagram and phasor diagram.

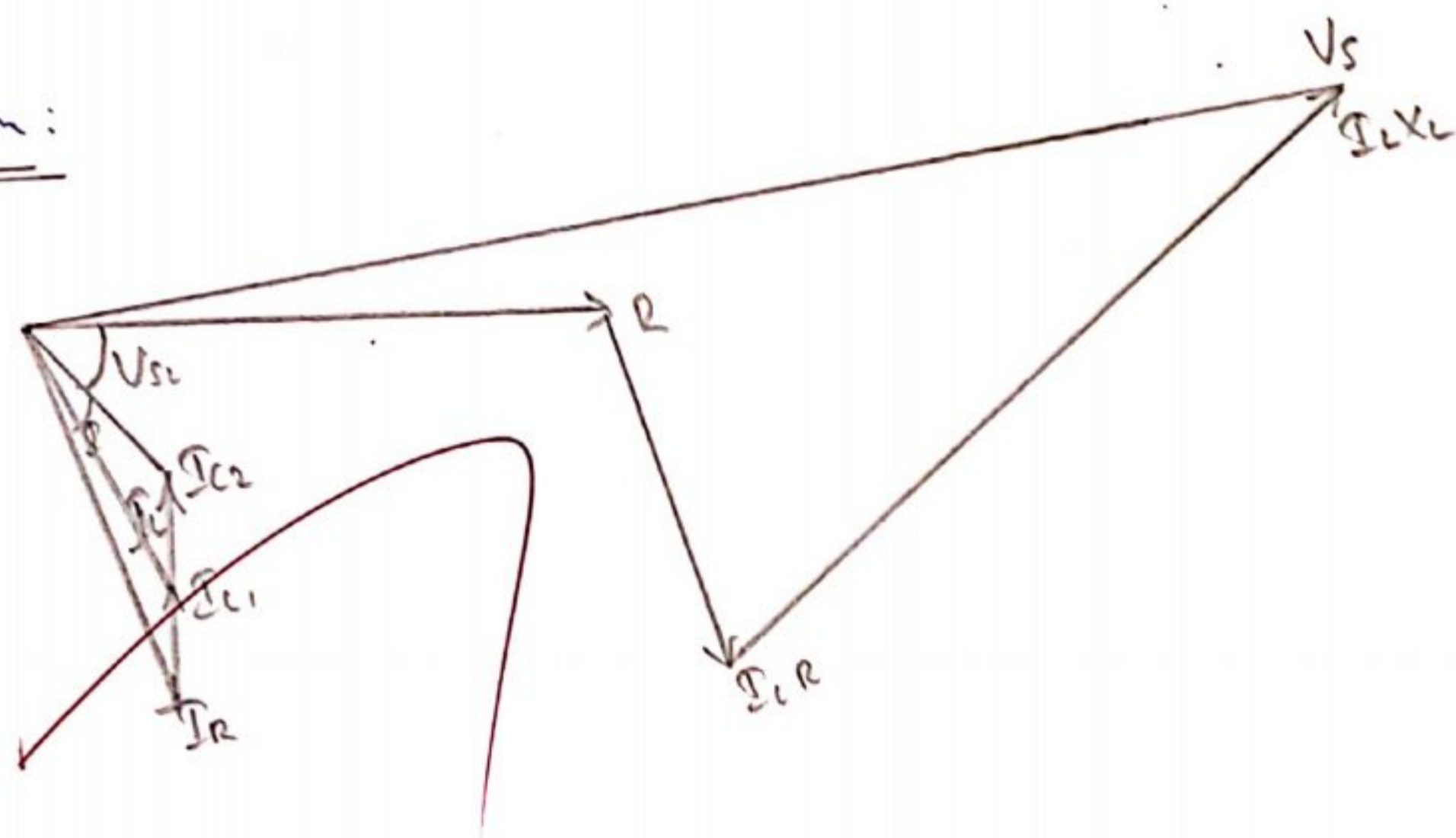


3. Explain the medium π method with neat diagram and phasor diagram:



Let, $V_R \Rightarrow$ Receiving end voltage
 $I_R \Rightarrow$ load current
 $R \Rightarrow$ loop resistance
 $X_L \Rightarrow$ loop reactance

Phasor Diagram:



$$\vec{V}_R = \vec{V}_R (1 + j0)$$

$$\vec{I}_R = I_R (\cos\phi - j \sin\phi)$$

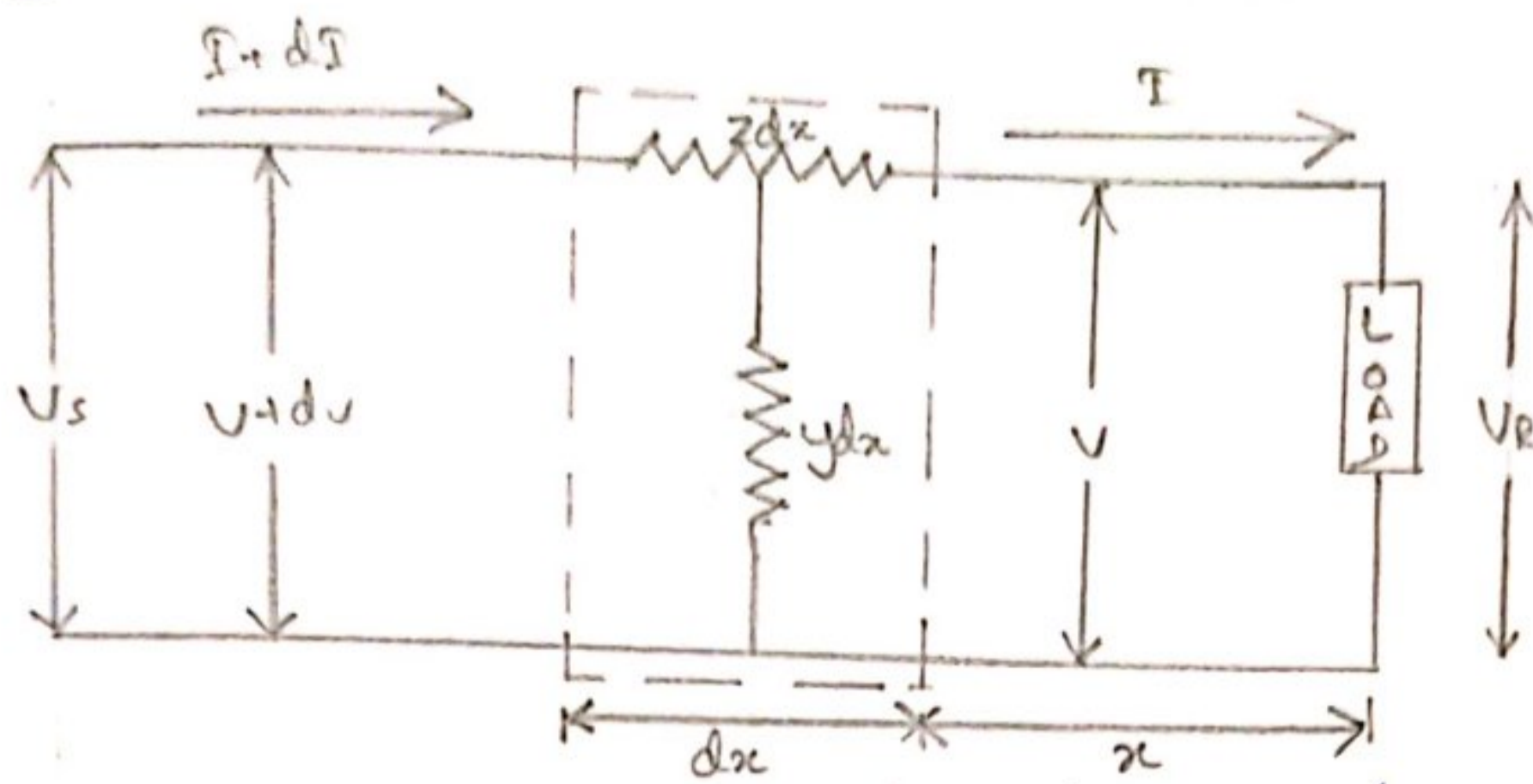
$$\vec{I}_{C1} = j\omega C/2 V_R = j2\pi f C/2 V_R$$

$$\vec{I}_{C2} = j2\pi f C/2 V_R$$

$$\vec{V}_S = \vec{V}_R + \vec{I}_R (R + jX_L)$$

$$\vec{V}_S = \vec{V}_R + \vec{I}_R (R + jX_L)$$

Explain the long transmission line (Rigorous method) with neat diagram.



Consider a small element in line length of 2 'dx' situated at the distance x from the receiving end.

$$dV = I_2 dx$$

$$\frac{dV}{dx} = I_2 \quad \text{--- (1)}$$

$$dI = -V y dx$$

$$\frac{dI}{dx} = -V y \quad \text{--- (2)}$$

Differentiating equation (1)

$$\frac{d^2V}{dx^2} = z \frac{dI}{dx}$$

$$\frac{d^2V}{dx^2} = z y x \quad (\text{from (2)})$$

$$\frac{d^2V}{dx^2} = z y V = 0$$

Solution is,

$$V = k_1 \cosh(x \sqrt{yz}) + k_2 \sinh(x \sqrt{yz}) \quad \text{--- (3)}$$

Differentiate equation (3)

$$\frac{dV}{dx} = k_1 \sqrt{yz} \sinh(x \sqrt{yz}) + k_2 \sqrt{yz} \cosh(x \sqrt{yz})$$

from ①

$$I_2 = k_1 \sqrt{y_2} \sinh(x \sqrt{y_2}) + k_2 \sqrt{y_2} \cosh(x \sqrt{y_2})$$

$$I = k_1 \frac{\sqrt{y_2}}{2} \sinh(x \sqrt{y_2}) + k_2 \frac{\sqrt{y_2}}{2} \cosh(x \sqrt{y_2})$$

$$I = k_1 \sqrt{\frac{y}{2}} \sinh(x \sqrt{y_2}) + k_2 \sqrt{\frac{y}{2}} \cosh(x \sqrt{y_2}) \quad \text{--- ④}$$

To find k_1 and k_2

where, $x=0$, $U=U_R$, $I=I_R$

Sub in eqnt. ③ and ④

$$\text{③} \Rightarrow U_R = k_1$$

$$\text{④} \Rightarrow I_R = k_2 \sqrt{\frac{y}{2}} \Rightarrow k_2 = I_R \sqrt{\frac{2}{y}}$$

$$\text{③} \Rightarrow U = U_R \cosh(x \sqrt{y_2}) + I_R \sqrt{\frac{2}{y}} \sinh(x \sqrt{y_2}) \quad \text{--- ⑤}$$

$$\text{④} \Rightarrow I = U_R \sqrt{\frac{y}{2}} \sinh(x \sqrt{y_2}) + I_R \cosh(x \sqrt{y_2})$$

when,

$$U=U_S, \quad I=I_S, \quad x=1$$

$$\text{⑤} \Rightarrow U_S = U_R \cosh(1 \sqrt{y_2}) + I_R \sqrt{\frac{2}{y}} \sinh(1 \sqrt{y_2})$$

$$\text{⑥} \Rightarrow I_S = U_R \sqrt{\frac{y}{2}} \sinh(1 \sqrt{y_2}) + I_R \cosh(1 \sqrt{y_2})$$

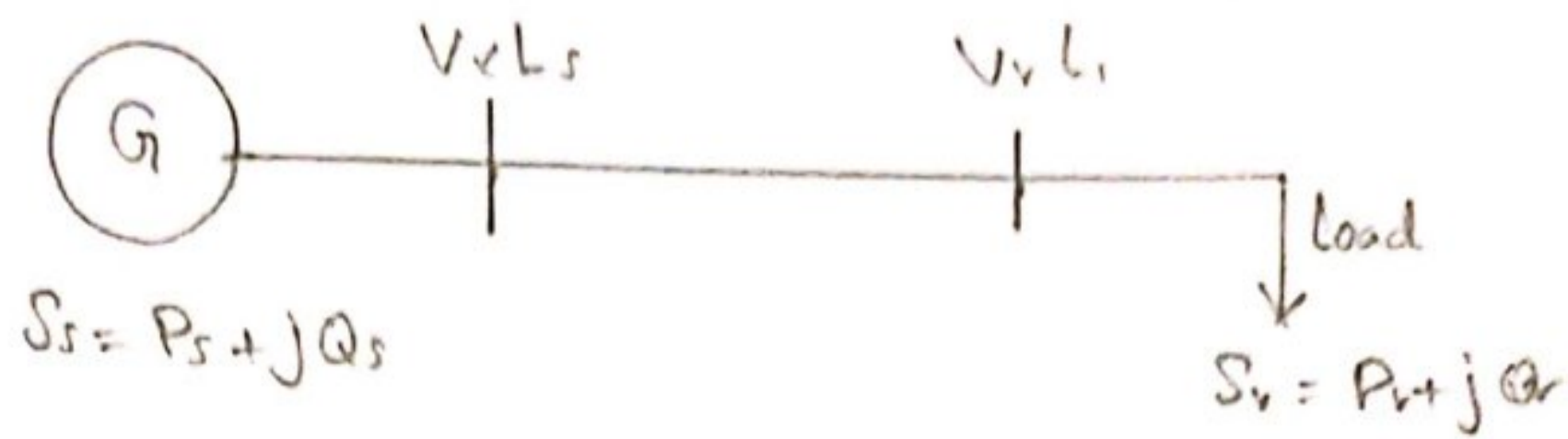
let

$$x = x_1, \quad y = y_1, \quad z = z_1$$

$$U_S = U_R \cosh \sqrt{y_2} + I_R \sqrt{\frac{2}{y}} \sinh \sqrt{y_2}$$

$$I_S = U_R \sqrt{\frac{y}{2}} \sinh \sqrt{y_2} + I_R \cosh \sqrt{y_2}$$

Refer the receiving end and sending end power cycle diagram with neat sketches and procedure.



Let,
 V_s, V_r = sending and Receiving end voltage
 I_s, I_r = Sending and Receiving end current
 P_s, P_r = Sending and Receiving end real power
 Q_s, Q_r = sending and Receiving end reactive power

$$\vec{V}_s = \vec{A}V_r + \vec{B}I_r \quad \text{--- (1)}$$

$$\vec{I}_r = \vec{C}V_r + \vec{D}I_s \quad \text{--- (2)}$$

Take, $\vec{A} = |A| \angle \alpha$, $\vec{B} = |B| \angle \beta$, $\vec{C} = |C| \angle \gamma$

$$\vec{V}_s = |V_s| \angle \delta, \quad \vec{V}_r = |V_r| \angle \phi$$

$$\text{(1)} \Rightarrow \vec{I}_r = \frac{|V_s| \angle \delta - \frac{|A| |V_r| \angle \alpha - \beta}{|B|}}{|B|}$$

$$\vec{I}_r = \frac{|V_s| \angle \delta - \frac{|A| |V_r| \angle \alpha - \beta}{|B|}}{|B|} \quad \text{--- (3)}$$

$$\vec{V}_r = \vec{D} \vec{V}_s - \vec{B} \vec{I}_s \quad \text{--- (4)}$$

$$\vec{I}_r = -\vec{C} \vec{V}_s + \vec{A} \vec{I}_s \quad \text{--- (5)}$$

$$\text{(4)} \Rightarrow \vec{I}_s = \frac{|D| |V_s| \angle \delta + \phi - \frac{|V_r| \angle \alpha}{|B|}}{|B|}$$

$$\vec{I}_s^* = \frac{|D| |V_s| \angle \delta - \alpha - \phi}{|B|} - \frac{|V_r| \angle \alpha}{|B|} \quad \text{--- (6)}$$

Complete power phase at sending end

$$S_s = P_s + jQ_s$$

$$S_s = \frac{|D| |V_s|^2 \angle \delta - \alpha}{|B|} - \frac{|V_s| |V_r| \angle \alpha - \delta}{|B|} \quad \text{--- (7)}$$

Receiving End:

$$S_r = \frac{|V_s| |V_r|}{|B|} \angle \phi - \delta - \frac{|A| |V_r|^2}{|B|} \angle \phi - \alpha \quad \text{--- (8)}$$

Real and reactive power

$$\textcircled{2} \Rightarrow S_r + P_r + jQ_r$$

$$P_r = \frac{|A| |V_r|^2}{|B|} \cos(\phi - \alpha) - \frac{|V_s| |V_r|}{|B|} \cos(\phi - \delta) \quad \text{--- (9)}$$

$$Q_r = \frac{|A| |V_r|^2}{|B|} \sin(\phi - \alpha) - \frac{|V_s| |V_r|}{|B|} \sin(\phi - \delta) \quad \text{--- (10)}$$

$$\textcircled{3} \Rightarrow S_r = P_r + jQ_r$$

$$P_r = \frac{|V_s| |V_r|}{|B|} \cos(\phi - \delta) - \frac{|A| |V_r|^2}{|B|} \cos(\phi - \alpha) \quad \text{--- (11)}$$

$$Q_r = \frac{|V_s| |V_r|}{|B|} \sin(\phi - \delta) - \frac{|A| |V_r|^2}{|B|} \sin(\phi - \alpha) \quad \text{--- (12)}$$

Power circle diagram:

$$\left[P_r + \frac{|A| |V_r|^2}{|B|} \cos(\phi - \alpha) \right] = \left[\frac{|V_s| |V_r|}{|B|} \cos(\phi - \delta) \right] \quad \text{--- (13)}$$

$$\left[Q_r + \frac{|A| |V_r|^2}{|B|} \sin(\phi - \alpha) \right] = \left[\frac{|V_s| |V_r|}{|B|} \sin(\phi - \delta) \right] \quad \text{--- (14)}$$

Square and add (13), (14)

$$\begin{aligned} & \left[P_r + \frac{|A| |V_r|^2}{|B|} \cos(\phi - \alpha) \right]^2 + \left[Q_r + \frac{|A| |V_r|^2}{|B|} \sin(\phi - \alpha) \right]^2 \\ &= \left[\frac{|V_s| |V_r|}{|B|} \cos(\phi - \delta) \right]^2 + \left[\frac{|V_s| |V_r|}{|B|} \sin(\phi - \delta) \right]^2 \end{aligned}$$

$$= \left| \frac{U_s / U_r}{|B|} \right|^2$$

This is a circle equation with centre point

$$X_c = \frac{|A| |U_r|^2}{|B|} \cos(\phi - \alpha)$$

$$Y_c = \frac{-|A| |U_r|^2}{|B|} \sin(\phi - \alpha)$$

$$r = \frac{|U_s| |U_r|}{|B|}$$

Procedure :

(*) Locate the centre of the circle O , on the x, y plain.

(*) With radius $\left(\frac{|U_s| |U_r|}{|B|} \right)$, draw an arc of circle from O .

(*) With an angle ϕ , draw a line from the origin which intersects the circle at M .

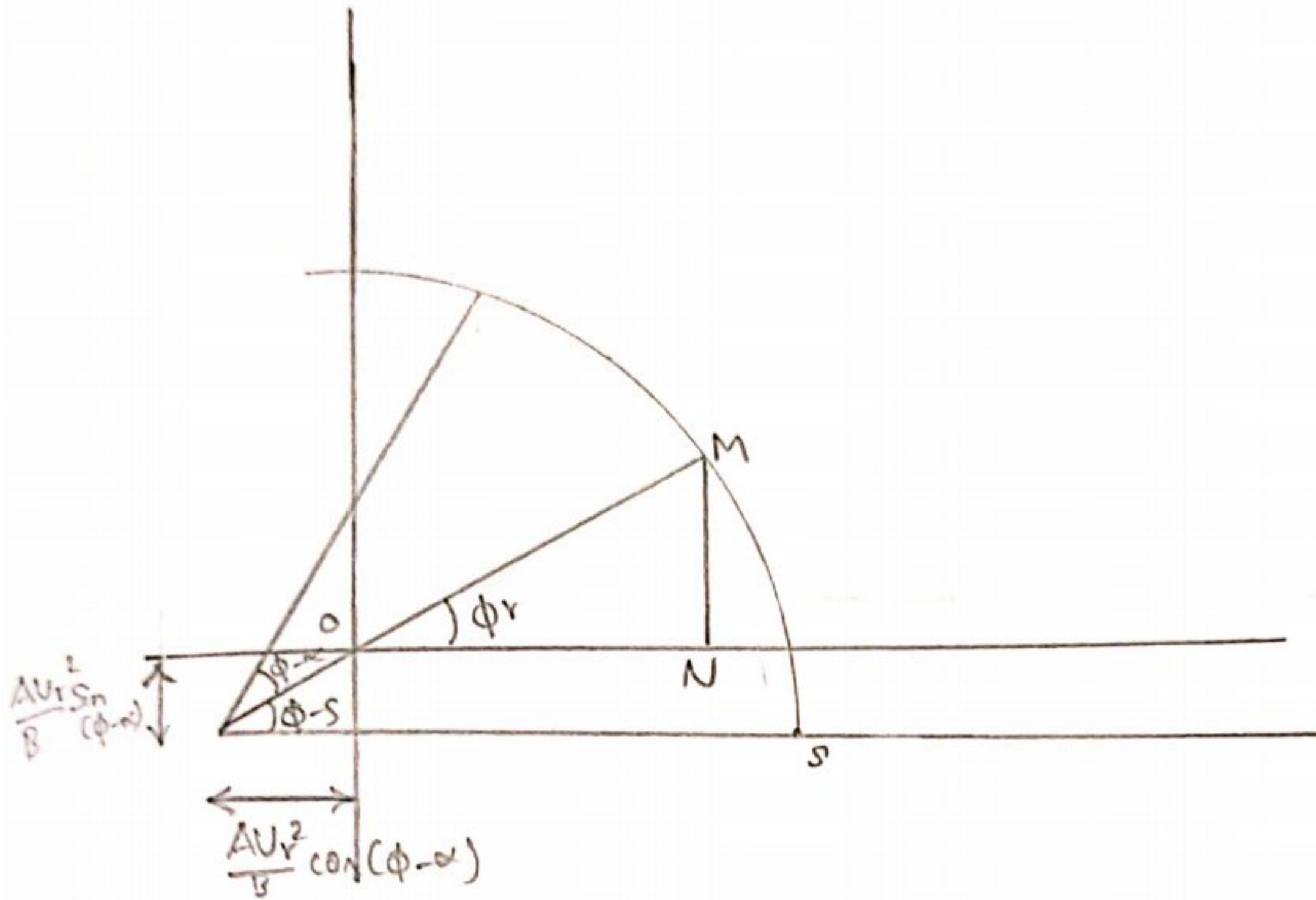
(*) Draw a perpendicular line at x -axis at N which centre sets the circle point M .

(*) From the centre of circle (O_1) draw a line parallel to x -axis line which intersects the circle at O and also the vertical axis at I .

S, C represent the maximum power.

(*) Draw a line between O_1 and O at angle $(\phi - \alpha)$

(*) Draw a line from O , to m and
 its angle is $(\phi - \alpha)$



Sending end power cycle diagram :

(*) Locate the centre of circle O_1 and x, y plane.

(*) With radius $\frac{VsVr}{B}$, draw an arc of circle from O_1 ,

(*) with an angle of ϕ_r , draw a line from origin which intersects the circle at M .

(*) Draw a line perpendicular to x axis which cuts in N .

M, N reactive power, ON real or active power.

(*) From O , draw a line horizontal to x -axis.

